



CSN08704

Telecommunications

4. Analysis of Digital Pulses

Data, Audio, Video and Images

<http://asecuritysite.com/comms>

Prof Bill Buchanan



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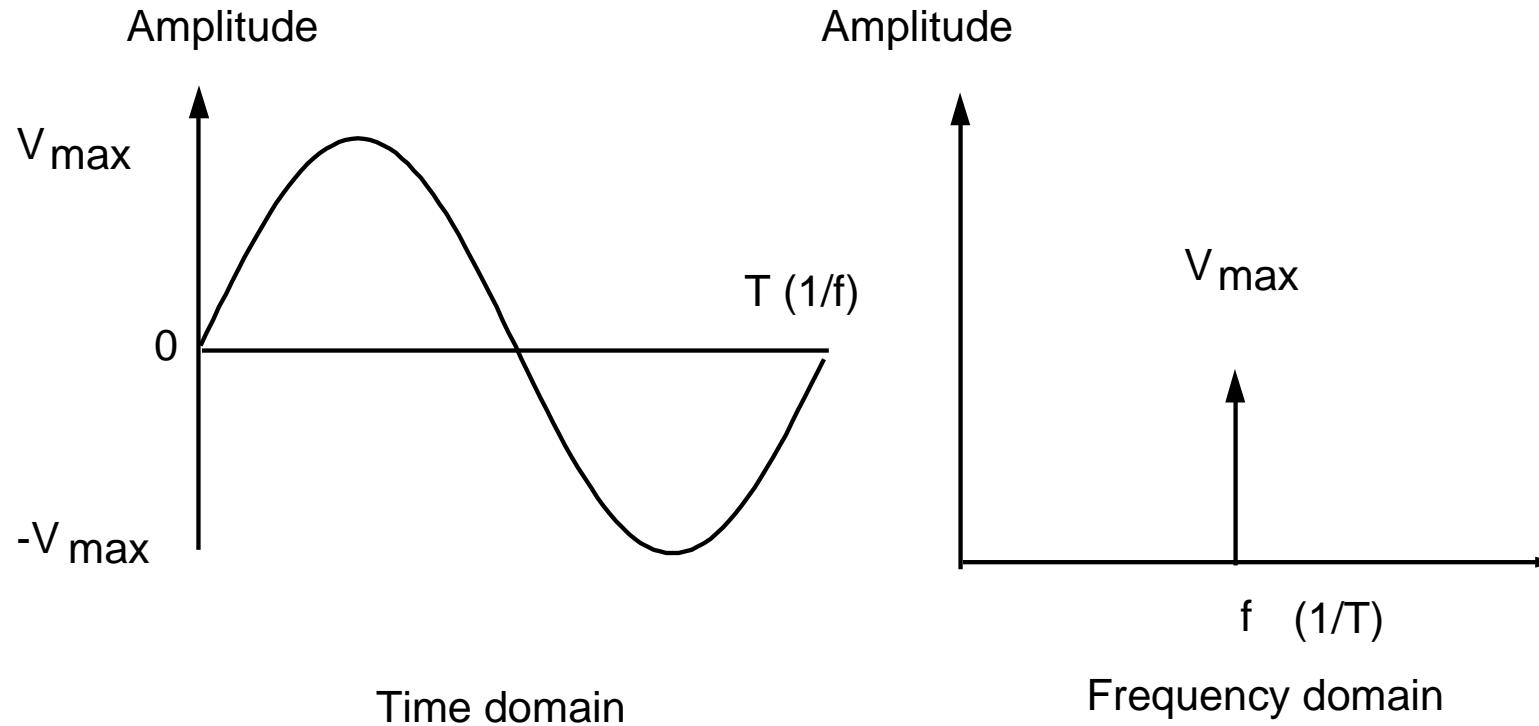
4. Analysis of Digital Pulses: Frequency and Time Domain

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Signals



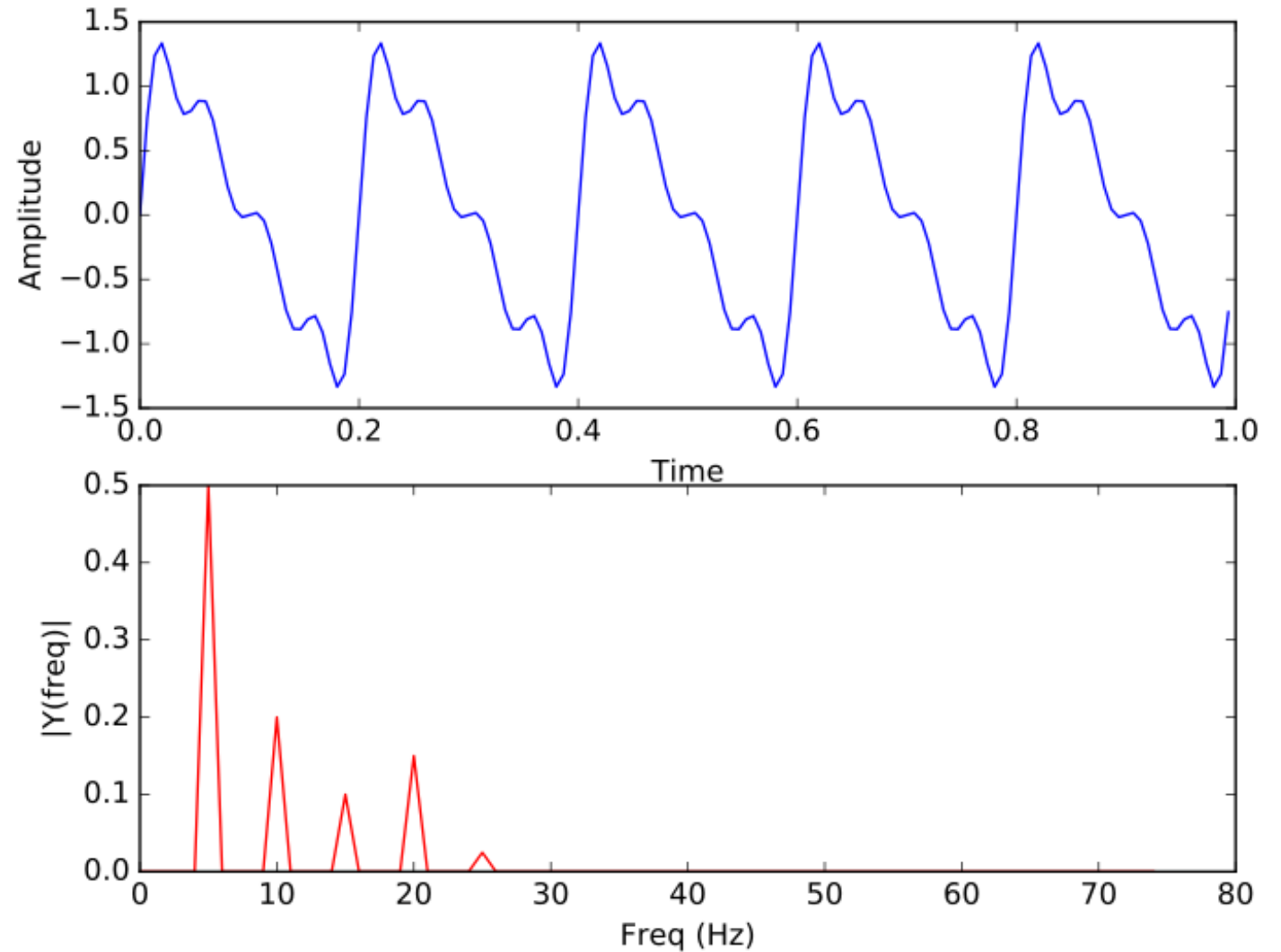
$$V(t) = V \sin(2\pi ft + \theta)$$

Repetitive Signals

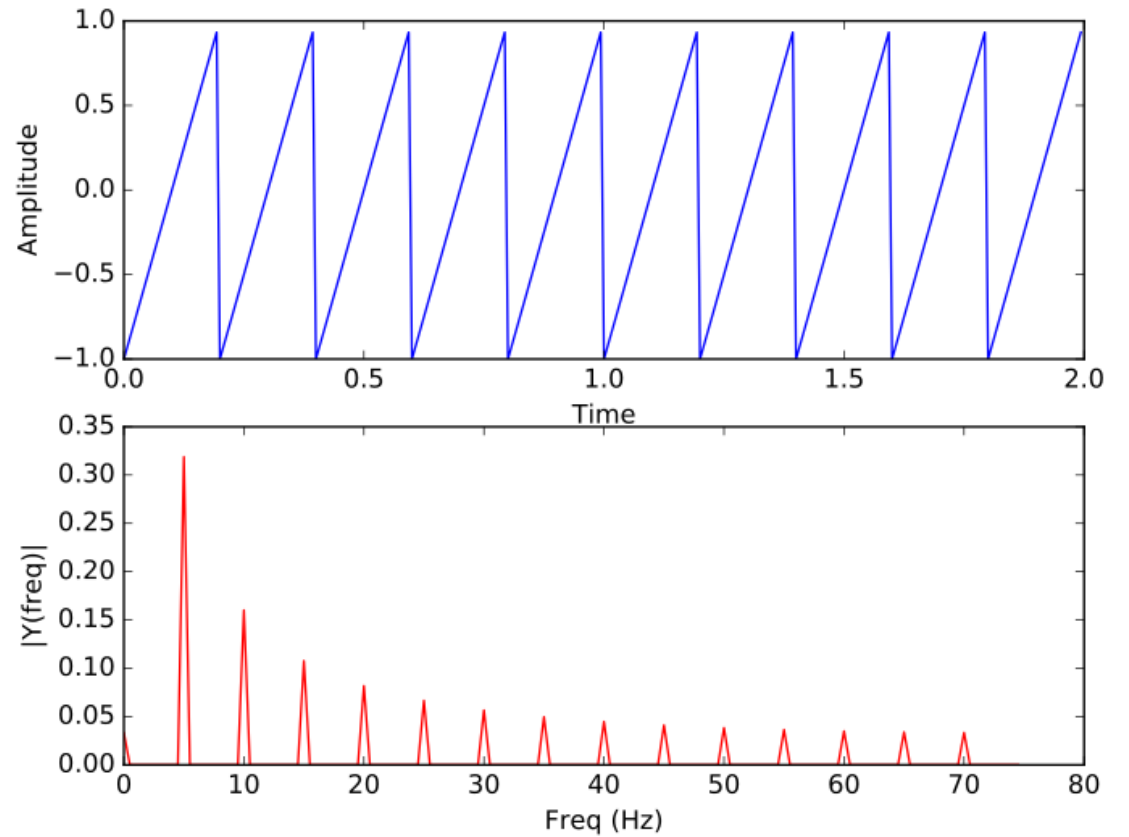
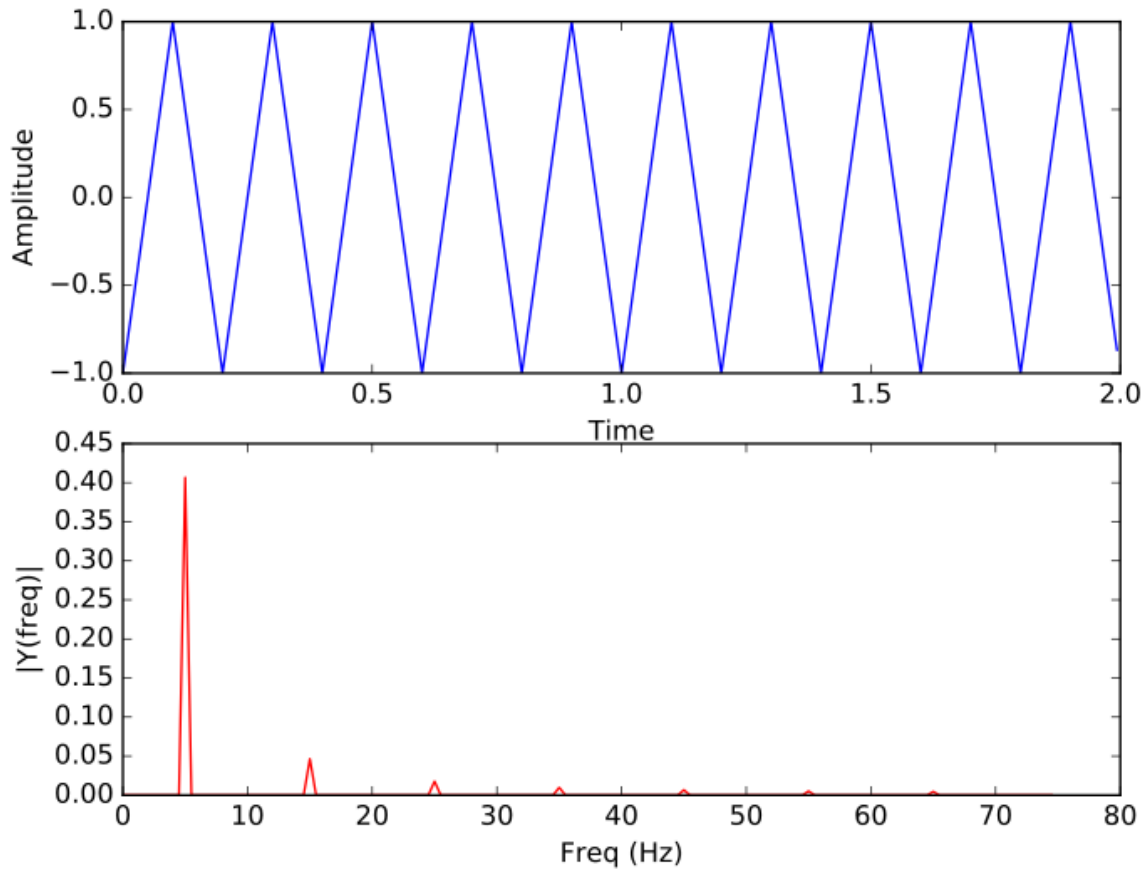
$$f(t) = A_0 + A_1 \cos \omega_1 t + A_2 \cos 2\omega_1 t + \dots + A_N \cos N\omega_1 t \\ + B_1 \sin \omega_1 t + B_2 \sin 2\omega_1 t + \dots + B_N \sin N\omega_1 t$$

Repetitive Signals

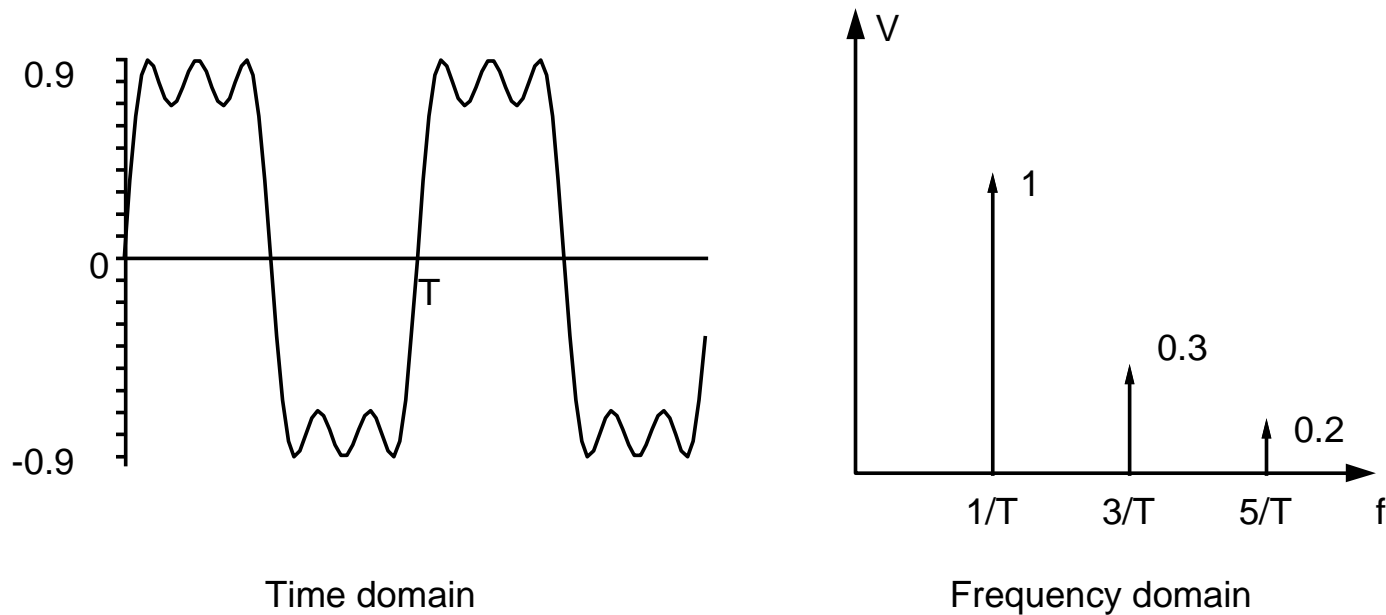
- 1 1st, 0.4 2nd, 0.2 3rd.
- 0.4 4th, 0.05 5th.
- [Link](#).



Repetitive Signals

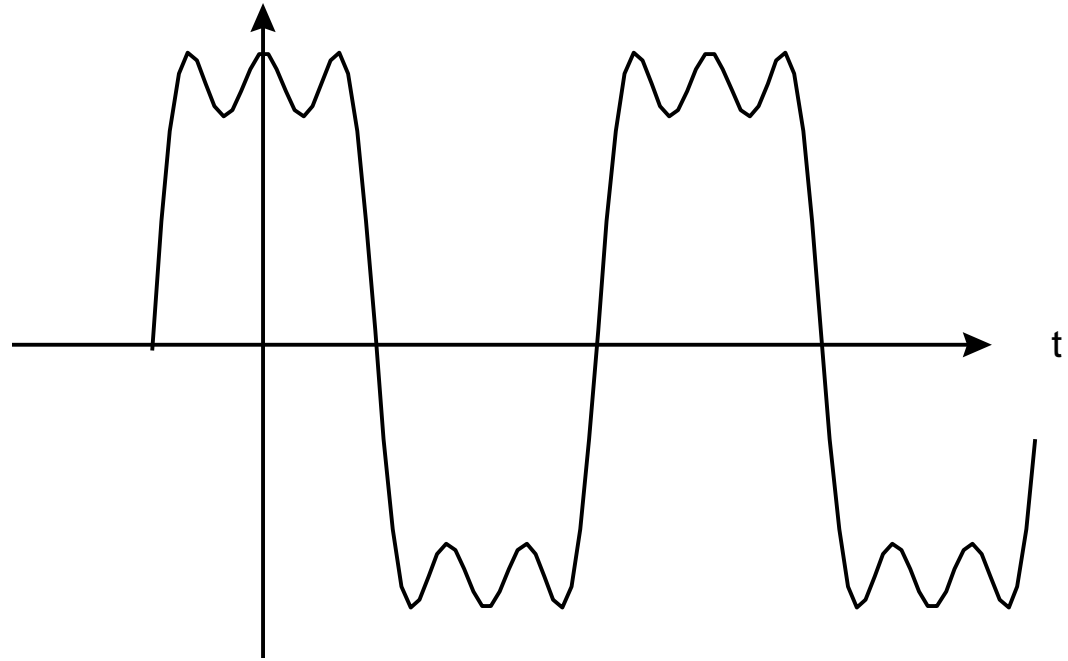


Example



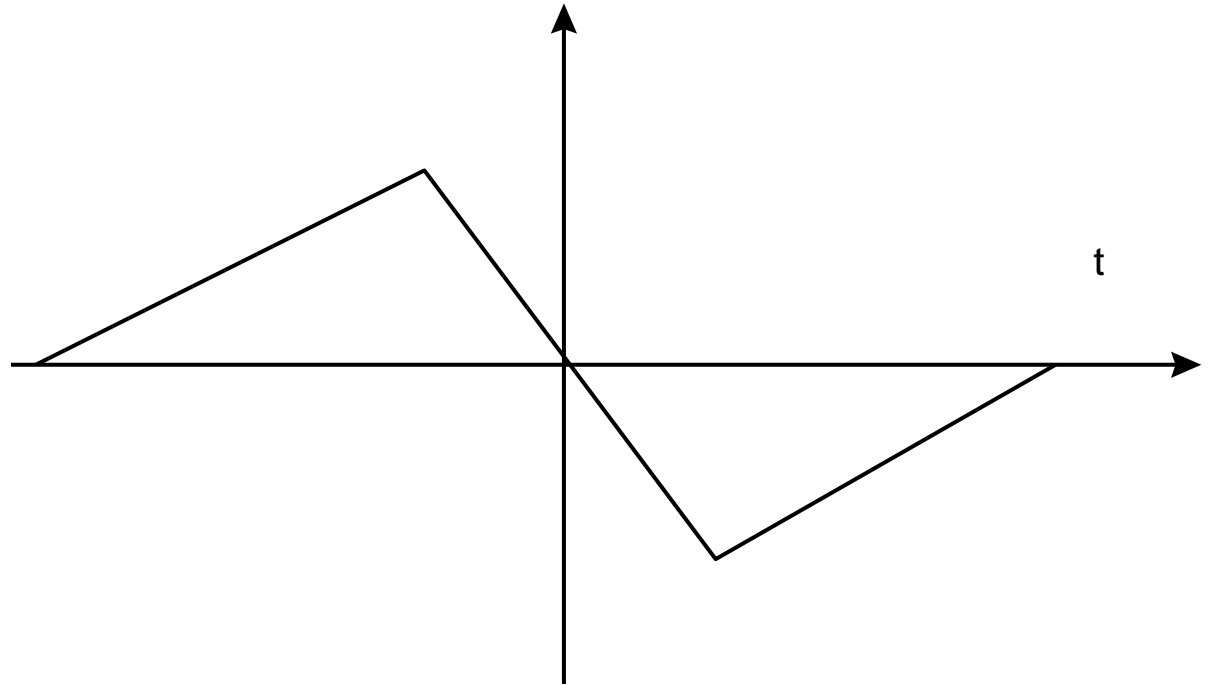
$$f(t) = \sin(\omega_1 t) + 0.3 \sin(3\omega_1 t) + 0.2 \sin(5\omega_1 t)$$

Even Symmetry



$$f(t) = A_0 + A_1 \cos \omega_1 t + A_2 \cos 2\omega_1 t + \dots + A_N \cos N\omega_1 t$$

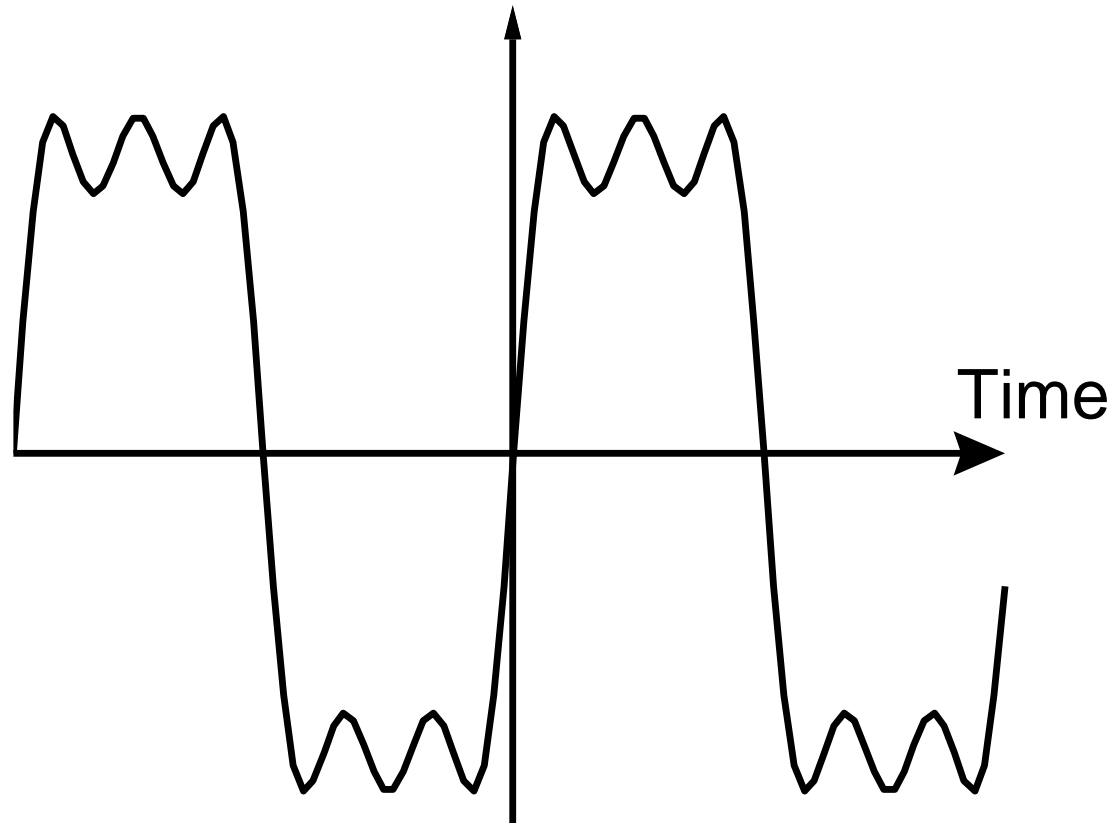
Odd Symmetry



$$f(t) = B_1 \sin \omega_1 t + B_2 \sin 2\omega_1 t + \dots + B_N \sin N\omega_1 t$$

Half Symmetry

- No even harmonics ... just odd harmonics.





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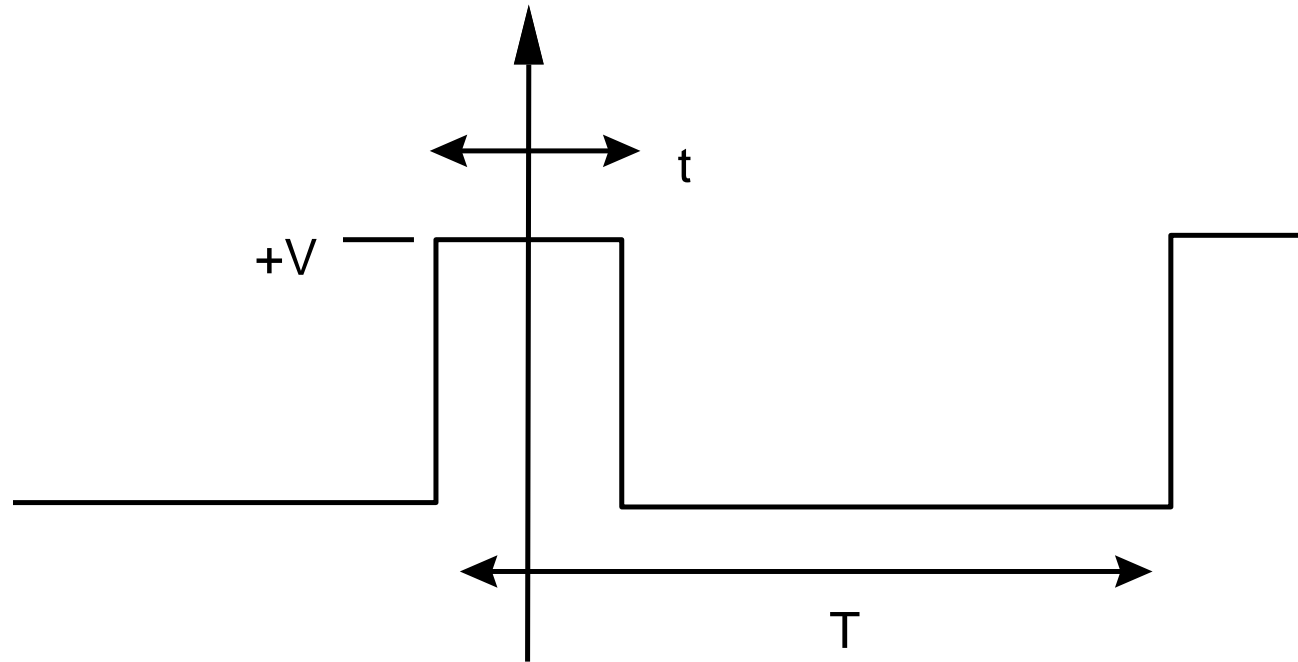
4. Analysis of Digital Pulses: Pulse Analysis

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Repetitive Pulse Stream

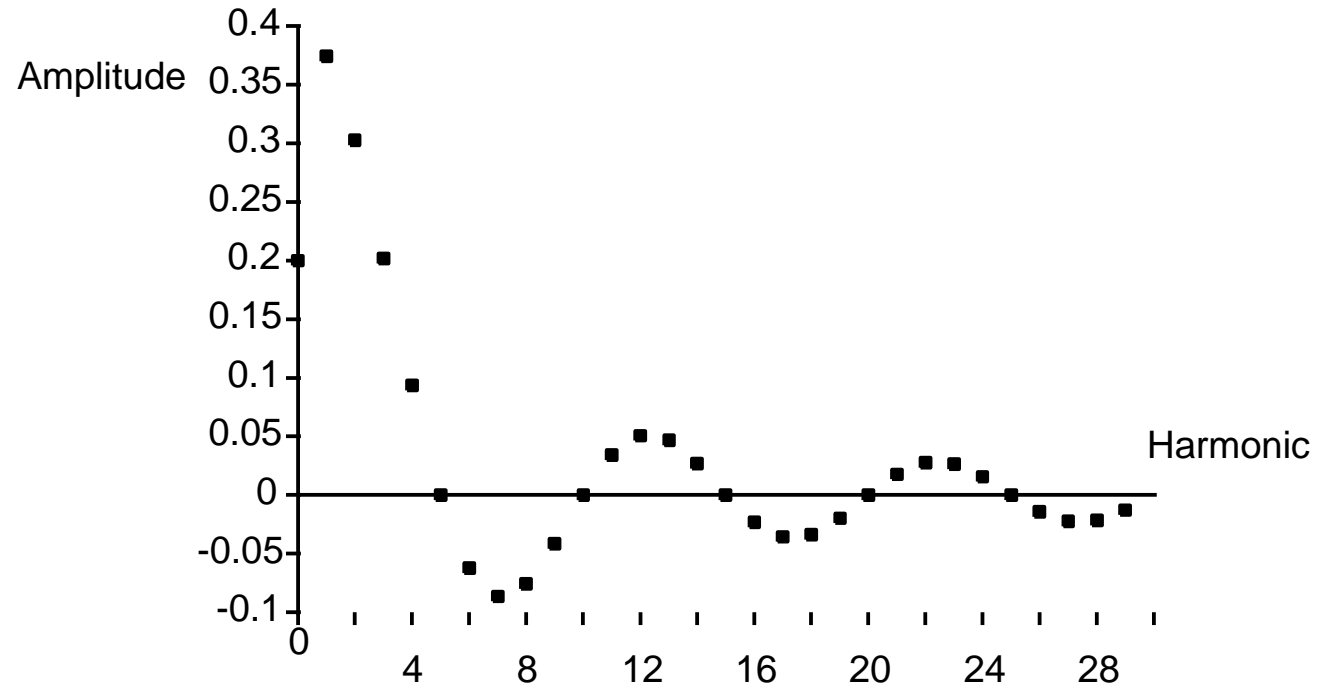
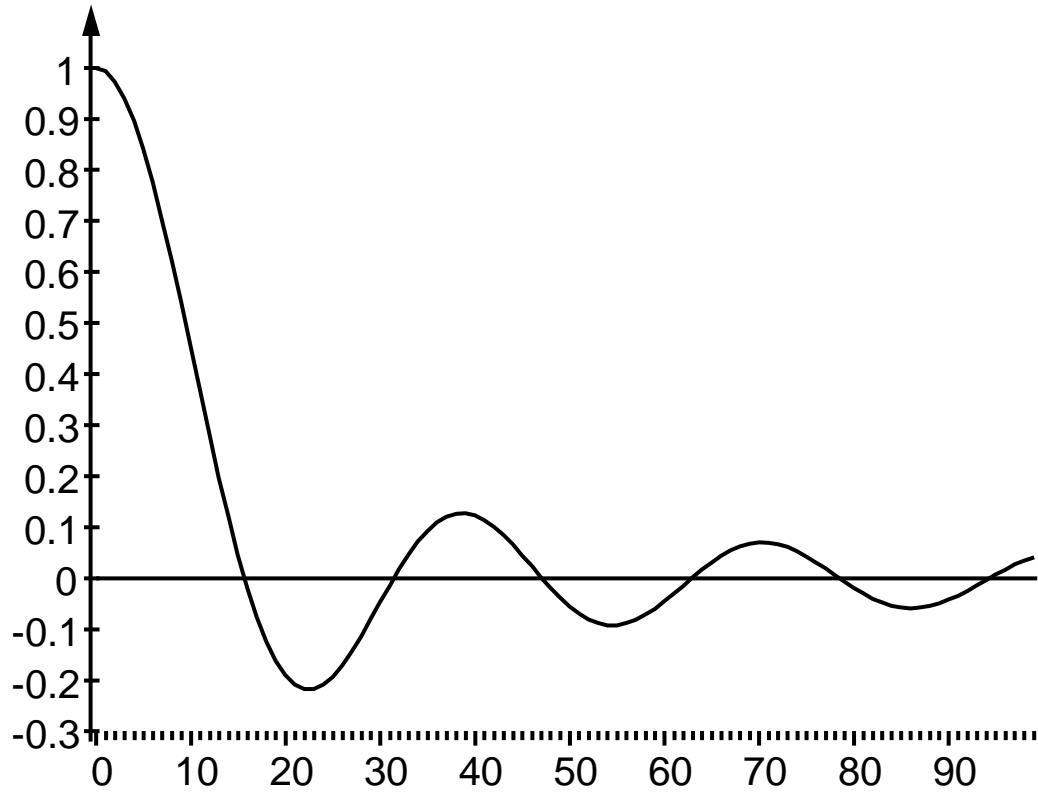


$$\text{Duty Cycle} = \frac{\tau}{T}$$

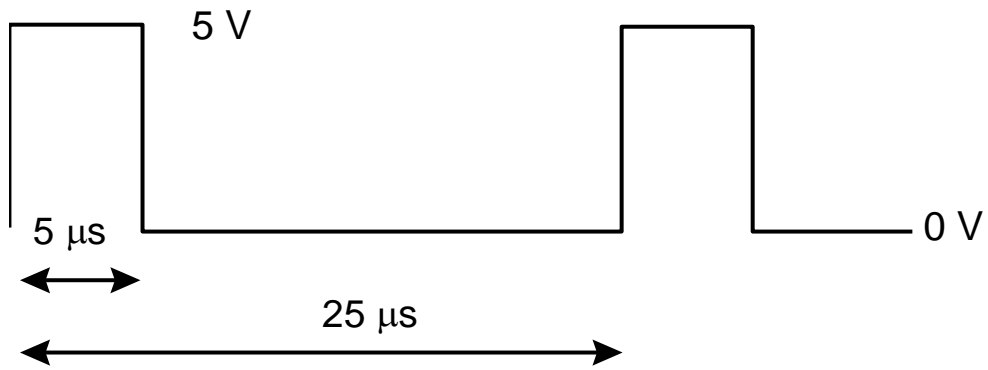
$$v(t) = \frac{V\tau}{T} + \sum_{n=1}^{n=\infty} V_n \cos(n2\pi f_1 t) \quad V_n = \frac{2V\tau}{T} \cdot \frac{\sin Nx}{x} \quad x = \frac{\pi\tau}{T}$$

Sin(x)/x

$$V_n = \frac{2V\tau}{T} \cdot \frac{\sin Nx}{x} \quad x = \frac{\pi\tau}{T}$$



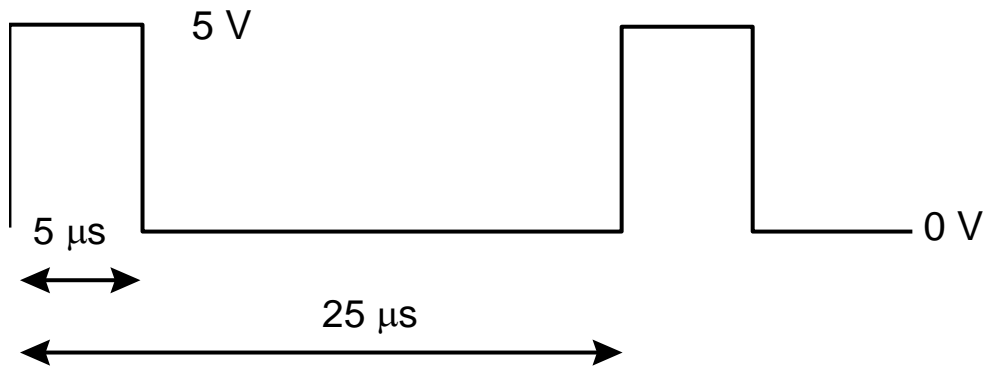
Worked Example



$$v(t) = \frac{Vt}{T} + \sum_{N=1}^{\infty} \left[\frac{2Vt}{T} \cdot \frac{\sin(N\pi t/T)}{N\pi t/T} \right] \cos(N\omega_1 t)$$

$$V_{DC} = V_{pk} \frac{t}{T} = 5 \cdot \frac{5}{25} = 1 \text{ V}$$

Worked Example



$$f_1 = \frac{1}{T} = \frac{1}{25 \times 10^{-6}} = 40 \text{ kHz}$$

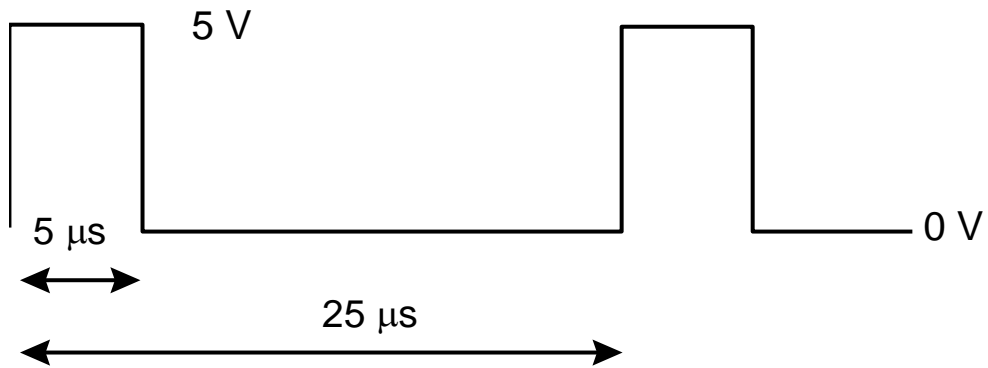
$$f_2 = 80 \text{ kHz}$$

$$f_3 = 120 \text{ kHz}$$

$$f_4 = 160 \text{ kHz}$$

$$f_5 = 200 \text{ kHz}$$

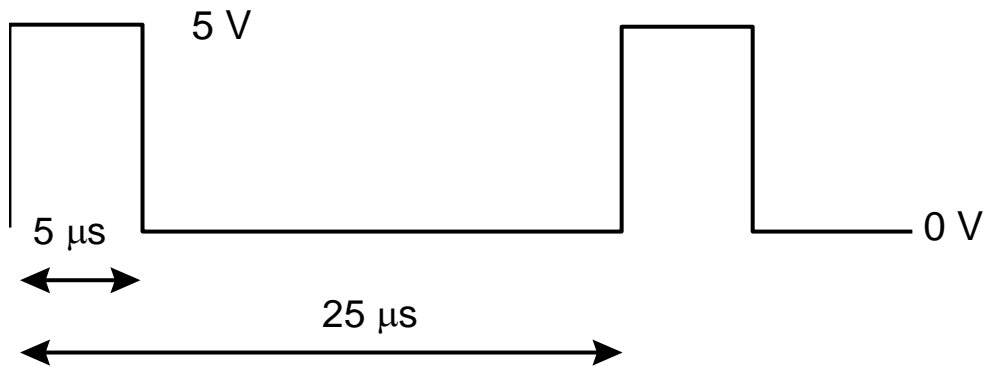
Worked Example



$$V_N = \frac{2Vt}{T} \cdot \frac{\sin(N\pi t/T)}{N\pi t/T}$$

$$\begin{aligned} V_N &= \frac{2 \times 5 \times 5}{25} \cdot \frac{\sin(0.2N\pi)}{0.2N\pi} \\ &= \frac{3.18}{N} \cdot \sin(0.63N) \quad \text{V} \end{aligned}$$

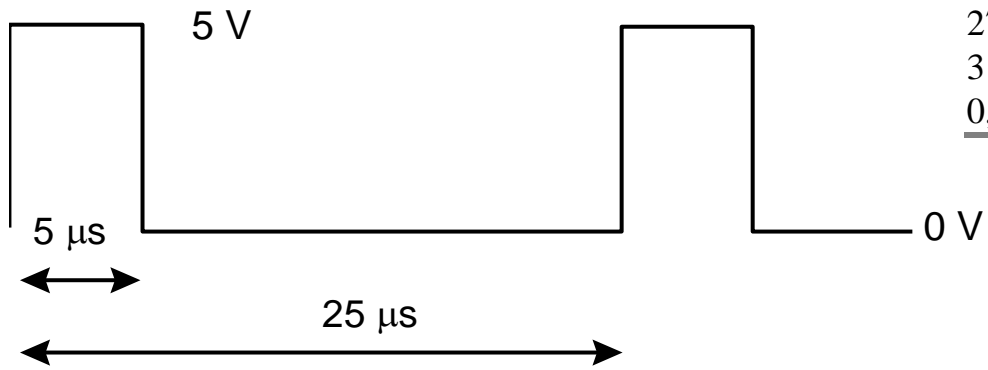
N	f (kHz)	V amplitude (Volts)
1	40	1.87
2	80	1.51
3	120	1.01
4	160	0.47
5	200	0



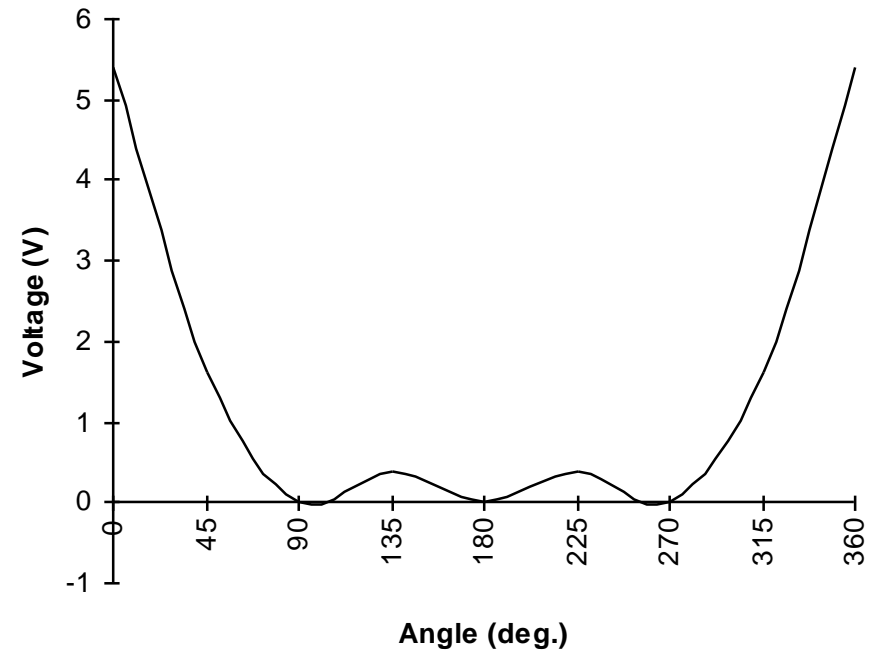
$$v_i(t) = 1 + 1.87 \sin(\omega_1 t) + 1.51 \sin(2\omega_1 t) + 1.01 \sin(3\omega_1 t) + 0.47 \sin(4\omega_1 t) + \dots$$

ωt (°)	V_0	V_1	V_2	V_3	Σ
	1	$1.77 \cos \omega t$	$1.51 \cos 2\omega t$	$1.01 \cos 3\omega t$	
45	1	1.32	0	-0.71	1.61
90	1	0	-1.51	0	-0.51
135	1	-1.32	0	0.71	0.39
180	1	-1.87	1.51	-1.01	-0.37
225	1	-1.32	0	0.71	0.39
270	1	0	-1.51	0	-0.51
315	1	1.32	0	-0.71	1.61
0,360	1	1.87	1.51	1.01	5.39

Worked Example

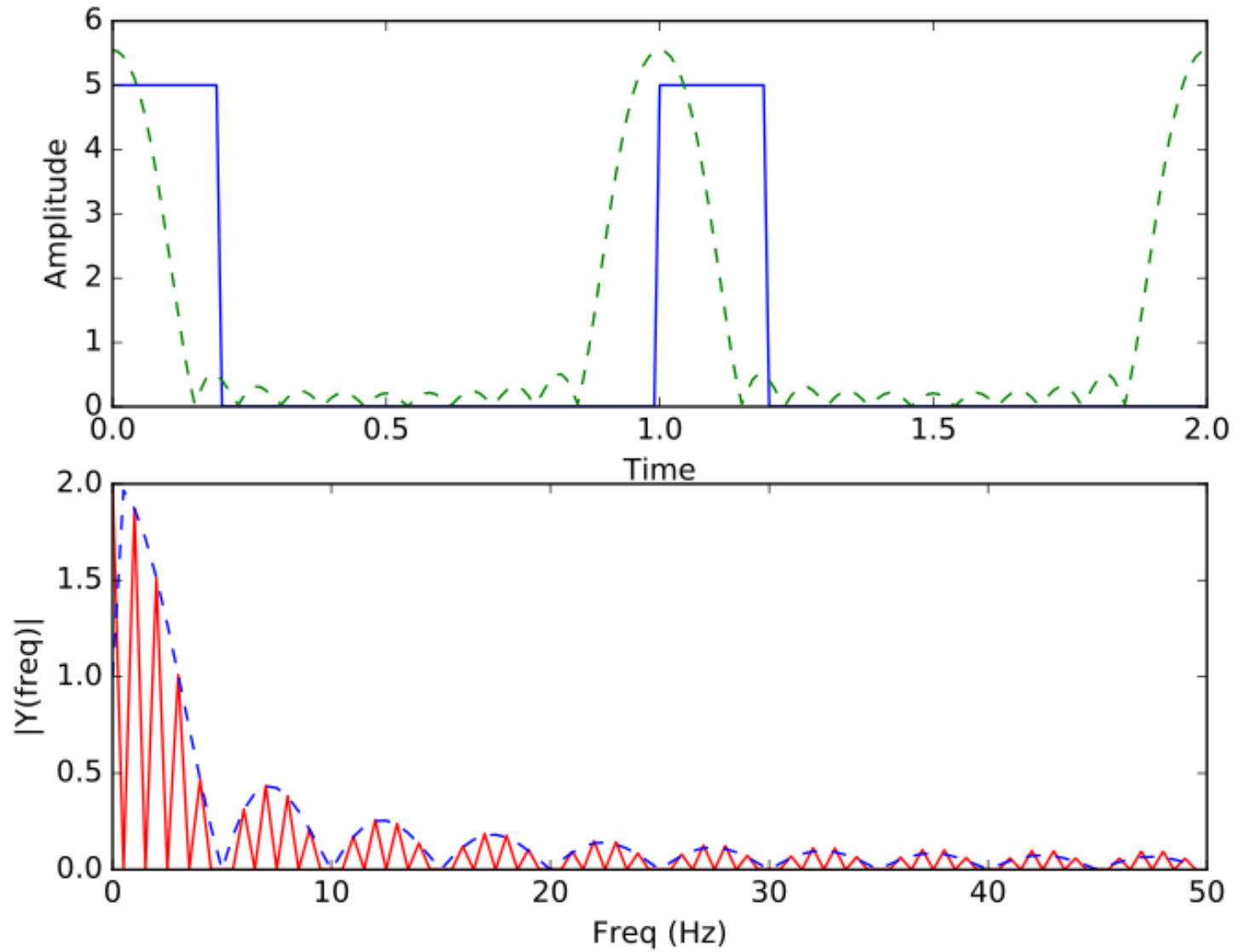


$\omega t (^\circ)$	V_0	V_1	V_2	V_3	Σ
	1	$1.77 \cos\omega t$	$1.51 \cos 2\omega t$	$1.01 \cos 3\omega t$	
45	1	1.32	0	-0.71	1.61
90	1	0	-1.51	0	-0.51
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0,360	1	1.87	1.51	1.01	5.39



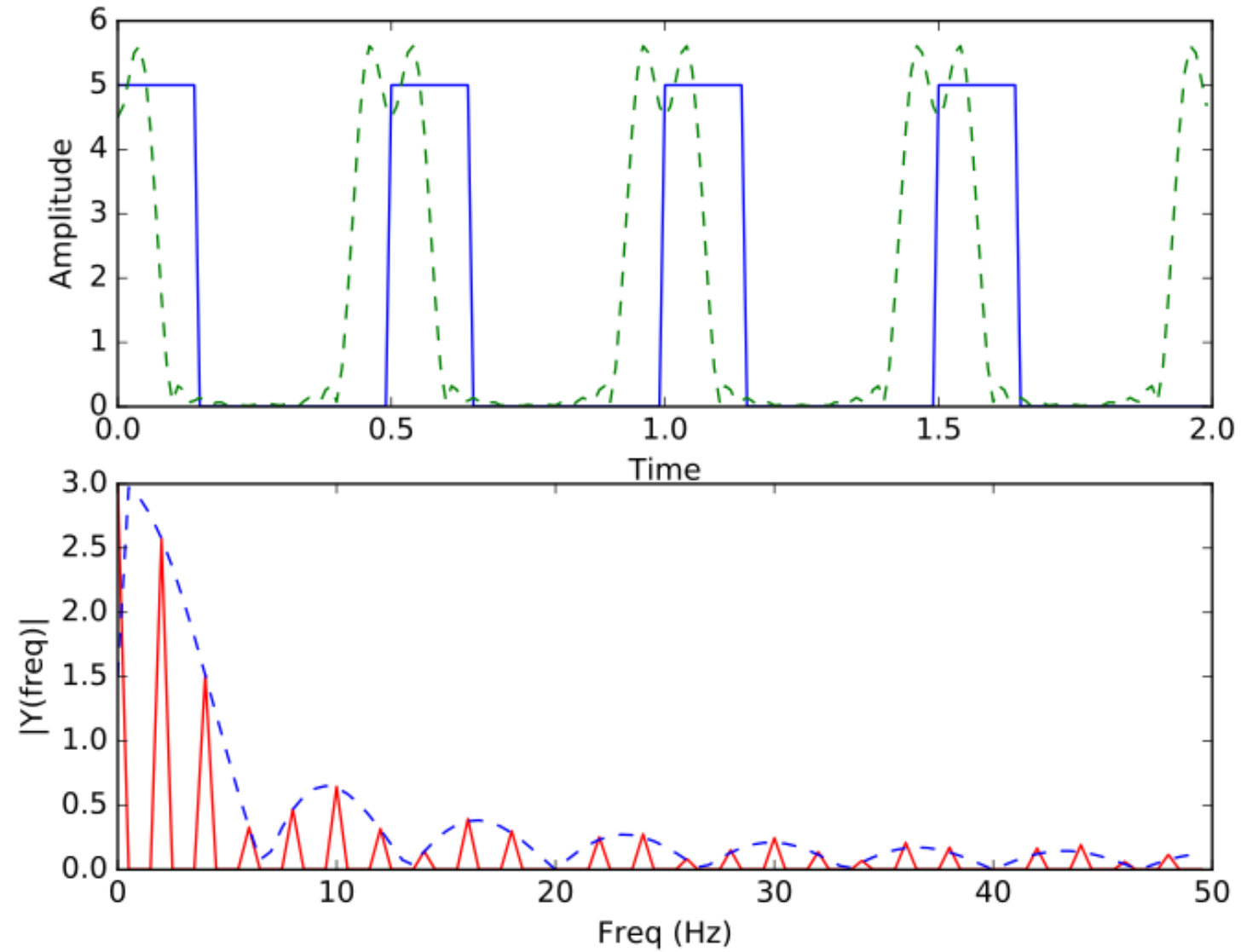
Example

- Duty cycle=0.2.
- [Link.](#)



Example

- Duty cycle=0.3.
- [Link.](#)





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